

Hi, I'm Greg. I'm a NYC tutor! I love helping students. I tutor many subjects, assist with homework help, etc. I mainly specialize in specialized tests.

As it turns out, I haven't been able to get to do as many livestreams as I have in past years (yet, hopefully that changes). Therefore, I thought it would be fun to start a Problem Of The Day Series. I will put up a problem and leave it running for a while. You guys will then analyze it, and come up with possible solutions and alternative solutions on your own. I'll eventually post the answer in some manner.

For now we'll play it by ear how that will happen and for how long I'll leave up a problem. But right now I'm thinking of keeping the problem up maybe 2 hours minimum and maybe even in some cases 4 or 5 hours depending upon the dynamics and my situation. Unlike my AMA (Ask Me Anything) livestream sessions, I will not be checking in every few minutes although I may from time to time join into the discussion. Again, the idea is for you guys to discuss out the problem.

Please be respectful to each other in this endeavor and let's make this fun, educational and forward-thinking. Keep the comments within the spirit of what I'm doing here. Please email me at GregsTutoringNYC@gmail.com if needed.

HERE'S THE PROBLEM: <—
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Round 199.9 times 1999 to the nearest unit.

- A) 400000 B) 399000 C) 399800 D) 399700 E) 399600

NOTE: You (should) all know how to solve this question.
But can you do it correctly the first go through?
Can you solve it in under 30 seconds?

HERE'S THE SOLUTION:
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If we want an estimate we can round up and have $200 \times 2000 = 400000$. But the answers choices given are too close together so we have to go a step further.

The most obvious knee-jerk approach is to just do the multi-digit multiplication, as we can round up or down once we get the product:

$$\begin{array}{r} 199.9 \\ \times 1999 \\ \hline 17991 \\ 17991 \\ 17991 \\ + 1999 \\ \hline \end{array}$$

3996001 accommodating the decimal point yields 399600.1 rounded is Choice E

That computation is error prone, tedious, and wastes time.

We can also look at this problem logically. If 1999 is one less than 2000 that's $1/2000$ less than the product therefore $400000/2000 = 200$ less overall. Similarly if 199.9 is $.1$ less than 200 that's $.1/200$ less than the product. Well $.1/200$ is also the same as $1/2000$ which we just computed therefore that's 200 less overall too. So we have $400000 - 400 = 399600$.

Note that in the computations in the previous paragraph we approached as 1999×200 and 199.9×2000 so we took too much away. We need to add back $1/2000 \times 1/2000 = 1/4000000 = 0.00000025$ and that multiplied by 400000 is $.1$ The answer choices don't care about a value that small.

Lastly, it seems the logical solution got somewhat carried away itself. Turns out that it

is actually accommodated mathematically/symbolically via the distributive property/FOIL.

This can apply to the problem at hand, that is, we see that

199.9 is the same as $200 - .1$
1999 is the same as $2000 - 1$

$$\begin{aligned} \therefore (200 - .1)(2000 - 1) &= 200 \times 2000 + 200 \times (-1) + (-.1) \times 2000 + (-.1)(-1) \\ &= 400000 - 200 - 200 + .1 \\ &= 399600.1 \text{ rounded is } \quad \text{Choice E} \end{aligned}$$

Use the math you know to your advantage! Once you see the FOIL you can often solve this problem in your head.

- Greg / GregsTutoringNYC@gmail.com LLAP ☺